

If I Had a set: $X = \{m,n,o,p,\dots\}$ whose number of elements were denoted as S , and I defined the following:

Let $X_S^{YYY\dots}$ Denote, if there are a Z count of Y 's, the summation of all the combinations of S elements

Taken Z at a time, where each element is raised to the power of Y .

ie...

If $X = \{a,b,c,d\}$, so $S = 4$, then:

$$X_4^{22} = \{a^2b^2 + a^2c^2 + a^2d^2 + b^2c^2 + b^2d^2 + c^2d^2\}$$

So its easy to see that the number of terms in the summation is equal to:

$$\#terms = [S!]/[(S-Z)!][Z!]$$

ie...

$$4!/2!2! = 6, \text{ which is the number of terms in that sum.}$$

So, lets say I had the Following:

$$X_4^{2,1} = \{a^2b + a^2c + a^2d + b^2a + b^2c + b^2d + \dots\}$$

The process by which I would calculate the #Terms seems to be the following:

$$(4!/[(4-1)!][1!]) * [(4-1)!/[(4-1)-1]!][1!]) ==> [4!/2!] = 12$$

Or, More Generally:

If we had:

$$X_S^{Y1,Y1\dots Y2,Y2\dots Y3,Y3\dots Y\dots}$$

Where $Z1 = \#Y1$'s, $Z2 = \#Y2$'s, ...

Then the count of the terms in the final summation would be:

$$[S!/(S-Z1)!(Z1!)] * [(S-Z1)!/(S-Z1-Z2)!(Z2!)] * [(S-Z1-Z2)!/(S-Z1-Z2-Z3)!(Z3!)] \dots$$

Or:

$$[S!/\{(S-Z1-Z2-Z3\dots!)*(Z1!)*(Z2!)*(Z3!)\dots\}]$$

For example, if we had $X = \{a,b,c,d,e,f\}$, and we wanted:

$$X_6^{2,1,1}$$

My Equation says there would be, since there is one 2, and Two ones,:

$$[6!/\{[6-1-2]!*[1!]*[2!]\}] = 6*5*4*3*2*1/3*2*1*1*2*1 = 6*5*4/2 = 60$$

Which represents the number of terms in:

$$\begin{aligned} & (\\ & a^2 * \{bc + bd + be + bf + cd + ce + cf + de + df + ef\} + \\ & b^2 * \{ac + ad + ae + af + cd + ce + cf + de + df + ef\} + \dots \\ &) \end{aligned}$$

Which as we see is indeed $6*10$ or 60 .